

## Pulsed Current-Carrying Capacity of Small Metallic Conductors as Applied to Device Test

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### Agenda

- Introduction
- Fourier's Law and Heat Transfer
- Pulsed Current Techniques
  - Steady-State vs. Pulsed Current Heating
  - Temperature Behavior in Conductors due to Pulsed Current
  - Transient Analysis
- Case Study: Power MOSFET
  - DUT Type and its Electrical Parameters
  - Heat Generation in DUT due to Applied Pulse of Energy
- Conclusions
- Glossary of Terms
- Appendices

## Introduction

- Objective of this Presentation:
  - To demonstrate Pulsed Current Thermal Techniques as applied to Electrical Conductors and Device Test
- Goal:
  - To provide a set of Guidelines to Users of the Methodology presented herein
- Future Work:
  - Expand on these Guidelines

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## Fourier's Law and Heat Transfer

### • Fourier's Equation in one dimension

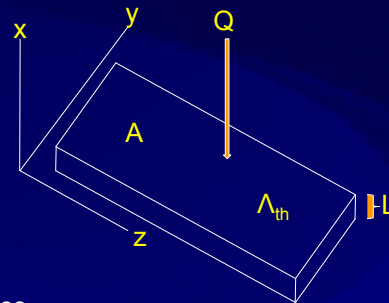
–General:  $(\partial^2 T / \partial x^2) = (c \cdot \rho / \Lambda_{th}) \cdot (\partial T / \partial t)$

- $\Lambda_{th}$  = specific thermal conductance
- $c$  = specific thermal capacitance
- $\rho$  = density of material
- $T$  = temperature
- $x$  = coordinates of heat conduction

### • Conductive Heat Transfer

–Specific:  $Q = -k \cdot A \cdot (\Delta T / L)$

- $Q$  = heat flux in Watts
- $k = \Lambda_{th}$  = specific thermal conductance
- $A$  = area through which heat is transferred
- $\Delta T$  = thermal rise across area of conductance
- $L$  = path length of thermal flow



Schematic of Heat Flow in Conductor

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### Steady-State vs. Pulsed Current Heating

- **Steady-State: 100% Duty Cycle – Static**
  - Consistent, internal heating of DUT and Contact Pins
  - $Q_{INT} = I^2R = m \cdot c_p \cdot \Delta T_{SS}$
  - $\Delta T_{SS} = I^2R / (m \cdot c_p)$
  - Obeys exponential law:  $\Delta T = \Delta T_{SS} \cdot (1 - e^{-t/\tau}) \rightarrow$  heating
- **Pulsed Current Heating: transient – Dynamic**
  - Duty cycle less than 100%
  - Single-shot pulse application
  - Multiple pulse application
  - High pulse currents for duty cycles <1%

### Temperature Behavior in Conductor during Steady-State Current Application

- Given a BeCu Contact with these parameters:
  - $R = 1.03 \times 10^{-3} \Omega$                       —  $m = 2.47 \times 10^{-7} \text{ Kg}$
  - $c_p = 418.7 \text{ J/Kg-K}$
  - $I = 1$  through 6 Amps applied current @ 100% DC
- Table of Current vs.  $\Delta T$  across Contact

DC (Amps)	Calc. $\Delta T$ (°C)	Meas. $\Delta T$ (°C)
1.0	+20.0	+20.0
2.0	+23.0	+24.0
3.0	+28.0	+29.0
4.0	+35.0	+38.0
5.0	+44.0	+47.5

## Temperature Behavior in Conductor During Pulse Current Application

- Heating of bond wires  $\approx$  transient heating of one-dimensional slab with a step change in energy generation rate
- CCC\* in wire follows same analysis as used for P-C conductors or wire-wrap interconnections

\*CCC = Current-Carrying Capacity (Amps)

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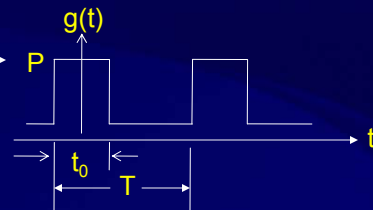
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## Temperature Behavior in Conductor During Pulse Current Application

- For a pulsed rectangular waveform

$$- P_{AV} = P * (t_0/T)$$

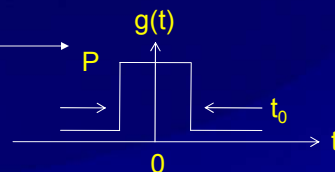
$$- P_{RMS} = P * (t_0/T)^{1/2}$$



- For a rectangular pulse

$$- g(t) = P \text{ for } (-t_0/2) < t < t_0/2$$

$$= 0 \text{ otherwise}$$



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## Temperature Behavior in Conductor During Pulse Current Application

- Given a BeCu Contact with these parameters:
  - $R = 1 \times 10^{-3} \Omega$                        $m = 1 \times 10^{-7} \text{ Kg}$
  - $P = 1 \times 10^{-3} \text{ Watts}$                        $c_p = 400 \text{ J/Kg-K}$
  - Conditions: Contact is a "free body" suspended in air
- At a current of 1 amp @ 100% duty cycle ( $t_0/T = 1$ )
  - $Q_{\text{int}} = I^2 R = m * C_p * \Delta T$
  - $\Delta T = (1^2 * 1 \times 10^{-3}) / (1 \times 10^{-7} * 400) = 25^\circ\text{C} \uparrow$
- If duty cycle = 50% ( $t_0/T = 0.5$ ) and peak power remains the same...
  - $I = 0.707 \text{ amps}$
  - $\Delta T = (0.707^2 * 1 \times 10^{-3}) / (1 \times 10^{-7} * 400) = 12.5^\circ\text{C} \uparrow$
  - Thus halving the duty cycle, halved the temperature rise

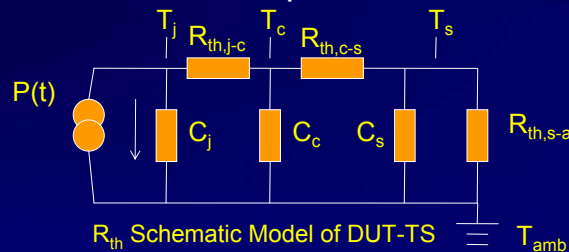
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## Transient Analysis

- Transient heating of DUT with 100% duty cycle current pulse
- DUT thermal resistance equivalent circuit diagram



$$-T_j = T_{SS} * [1 - \exp(-t / (R_{th,x} * C_{th,x}))]$$

$$-t = \text{time (sec)}$$

$$-R_{th,x} = \text{relative thermal resistance}$$

$$-C_{th,x} = \text{relative thermal capacitance}$$

$$-R_{th,x} * C_{th,x} = \text{time constant } (\tau)$$

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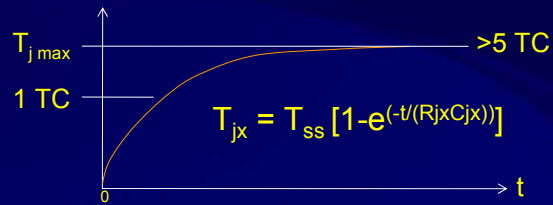
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## Transient Analysis

- Table & Graph of  $T_j$  vs. Time

1 TC =	63.2% $T_{SS}$
2 TC =	86.5% $T_{SS}$
3 TC =	95.0% $T_{SS}$
4 TC =	98.2% $T_{SS}$
5 TC =	99.3% $T_{SS}$



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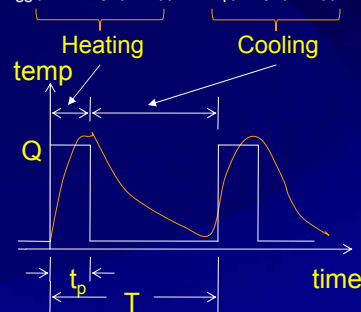
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## Transient Analysis Using Composite Thermal Equation

- Transient heating of DUT w/ low duty cycle current pulses
- Summation process built on alternate heating & cooling cycles

– Composite thermal equation:  $T_f = T_{amb} + T_{ss}(1 - \exp(-t/\tau)) + T_i(\exp(-t/\tau))$

- $T_f$  = final temp/cycle
- $T_i$  = temp at end of previous heat cycle
- $T_{amb}$  = ambient temperature
- $T_{ss}$  = overall steady-state temp
- $\tau$  = time constant



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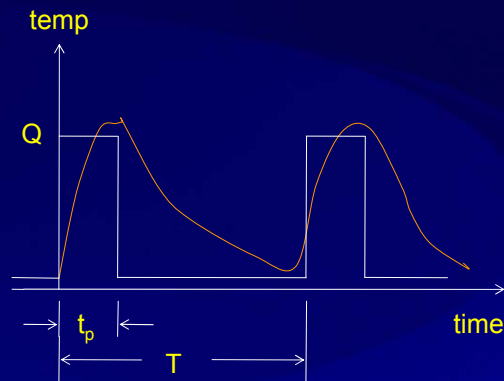
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## Transient Analysis Using Composite Thermal Equation

- Graph of heating vs. time

$$-T(t) = f(t) * R_{th} * Q$$

- $f(t)$  = thermal step function response
- $f(t_0) = 0$
- $f(t_{\infty}) = 1$
- $R_{th}$  = thermal resistance



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## Transient Analysis using Composite Thermal Equation

- A 10 Hertz square wave ( $P_{AVG} = 1W$ ) is applied to a DUT and cycled 5 times. What is the temperature of the die?

$$T_{amb} = +30^{\circ}C \quad R_{th} = 10^{\circ}C/W \quad T_{ss} = +60^{\circ}C$$

$$C_{th} = 0.01W\text{-sec}/^{\circ}C \quad T_{ON} = T_{OFF} = 0.05 \text{ sec} \quad TC = 0.10 \text{ sec}$$

### Table of Calculated Values

$T_1$	$60 * (1 - \exp(-0.05/0.10))$	= 23.6°C	Heating
$T_2$	$23.6 * (\exp(-0.5))$	= 14.3°C	Cooling
$T_3$	$14.3 + 60 * (1 - \exp(-0.05/0.10))$	= 37.9°C	Heating TC1
$T_4$	$37.9 * (\exp(-0.5))$	= 23.0°C	Cooling
$T_5$	$23.0 + 60 * (1 - \exp(-0.05/0.10))$	= 46.6°C	Heating
$T_6$	$46.6 * (\exp(-0.5))$	= 28.3°C	Cooling
$T_7$	$28.3 + 60 * (1 - \exp(-0.05/0.10))$	= 51.9°C	Heating TC2
$T_8$	$51.9 * (\exp(-0.5))$	= 31.5°C	Cooling
$T_9$	$31.5 + 60 * (1 - \exp(-0.05/0.10))$	= 55.1°C	Heating ~TC3
$T_{10}$	$55.1 * (\exp(-0.5))$	= 33.4°C	Cooling

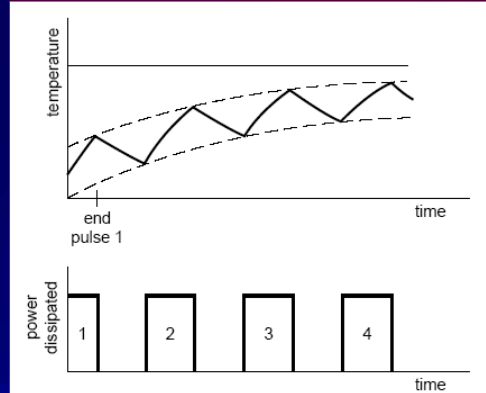
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## Transient Analysis

- Chart showing series of power pulses
  - Ref 1: Philips Semiconductor, *Thermal Considerations*, May 1999
  - Ref 2: Table of Calculated Values, Slide 14
- A train of power pulses increases  $T_{AVG}$  because the DUT doesn't have time to cool between pulses
  - Cf. Chart at right



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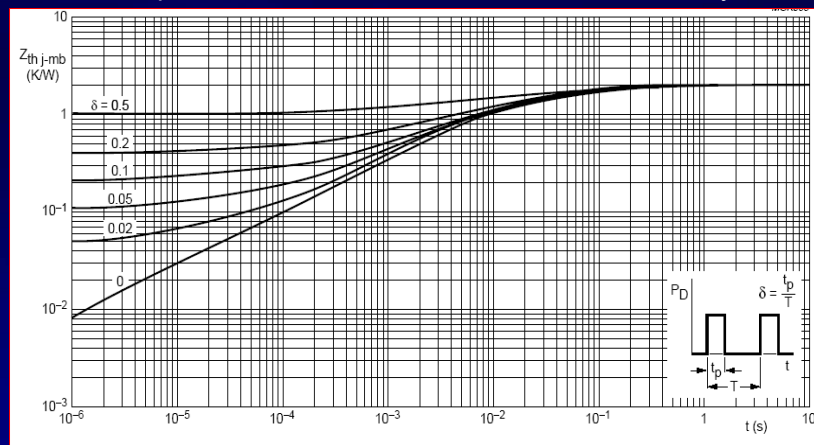
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## Transient Analysis

Graph of thermal impedance vs. pulse time/duty factor

Ref: Philips Semiconductor, *Thermal Considerations*, May 1999



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## Transient Analysis

### Things to consider when using Graph on previous slide

- If pulse time is very short:
  - Power dissipated doesn't have a limiting action
  - Pulse current and maximum voltage form the only limits
- A train of power pulses increases  $T_{AVG}$  :
  - DUT doesn't have time to cool between pulses
- Short pulses at low frequencies:
  - Lower the final temperature that the DUT junction reaches
- Peak junction temp usually occurs at end of applied pulse:
  - Its calculation will involve transient thermal impedance
- Avg. junction temp is calculated (if applicable) by using avg. power dissipation and the DC thermal resistance

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## Calculations using Data & Graph

- Calculate junction temp of DUT
  - Use a single-shot pulse
    - Peak current and voltage = 50 amps @ 20VDC for 100 microseconds
    - Pulse repeated after 20 seconds (Duty Cycle,  $\delta \sim 0$ )
    - $P_p = I \cdot E = 50 \cdot 20 = 1000$  Watts
    - $T_{mb} = +30^\circ\text{C}$
  - Use transient analysis for short duration pulse
    - $Z_{th,j-mb} = 1.8 \times 10^{-2}$  K/W (from graph on slide 16)
    - $\Delta T_{j-mb} = P \cdot Z_{th,j-mb} = 1 \times 10^3 \times 1.8 \times 10^{-2} = 18^\circ\text{C}$
    - $T_{j-peak} = T_{mb} + \Delta T_{j-mb} = 30 + 18 = +48^\circ\text{C}$

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### Calculations using Data & Graph

- Calculate junction temp of DUT, cont'd...
  - Salient facts gleaned from this high power application
    - Junction temp of device is not exceeded if pulse is...
      - Of short duration
      - Single-shot or low duty cycle

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### Case Study: Power MOSFET

Analytical procedure to determine junction temp of die subjected to a particular pulse width and peak power

- DUT type and its electrical parameters
- Test socket and contact pin data
- Contact pin, insert & IF parameter values
- Interface geometry for DUT-TS-LB
- Interface evaluation & thermal rise
- Heat generation in DUT & mounting base
  - Application of high power pulse to DUT
  - Temperature of mounting base
  - Temperature of junction of die

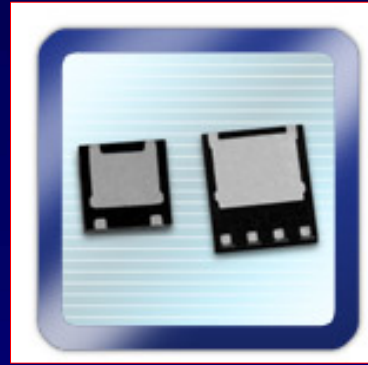
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## DUT Type and Electrical Parameters

- Package size: 3.3 x 3.3 mm, 0.65mm pitch, 8 pads
- Electrical parameters
  - $V_{IN} = 20V$ , max.
  - $I_{IN} = 40 A$ , max.
  - Specific heat  $\sim 200J/Kg-K$
  - Mass  $\sim 1 \times 10^{-4} Kg$
  - Electrical resistivity ( $R_e$ )  $\sim 1 \times 10^{-2} \Omega$
- Other
  - $R_{th, j-c} = 2.4^\circ C/W$
  - $C_{th, j-c} = 0.1W-sec/^\circ C$
  - $J_{T,max} = +175^\circ C$
  - $P_{DISS} (<10sec) = 3.8W$

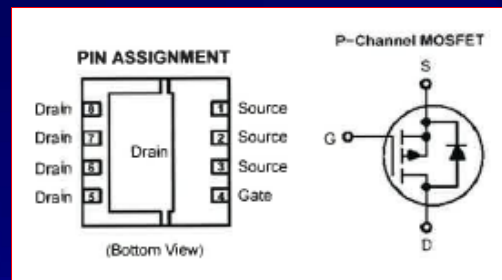


**Power QFN MOSFET**  
Courtesy: PSi Technologies

## Test Socket and Contact Pin Data

- Contact Pins: AuNi-plated BeCu – 8 req'd.
- Ground/Thermal Insert: Copper
- Surface of DUT leads: Matte Tin or NiPdAu-plated
- Force of DUT against Contacts at I.F.  $\sim 65$  grams/pin
- Typical Contactor pin-outs to pads of DUT

- Source: 3 pins
- Gate: 1 pin
- Drain: 4 pins



## Contact Pin, Insert & IF Data

### Calculated Contact Pin/Insert/IF values

Parameter	Calc. Value
$R_E$ (Contact Pin)	$7.0 \times 10^{-4} \Omega/\text{pin}$
$R_E$ (IF)	$1.3 \times 10^{-3} \Omega/\text{IF}$
$R_E$ (Contact Pin + IFs)	$3.3 \times 10^{-3} \Omega$
$R_E$ (Copper Insert)	$2.6 \times 10^{-6} \Omega$
$R_E$ (Copper Insert + IFs)	$3.9 \times 10^{-5} \Omega$
$R_{TH}$ (Contact Pin)	$142^\circ\text{C}/\text{W}$
$R_{TH}$ (Contact Pin + IFs)	$150^\circ\text{C}/\text{W}$
$R_E$ (Copper Insert)	$0.5^\circ\text{C}/\text{W}$
$R_E$ (Copper Insert + IFs)	$1.0^\circ\text{C}/\text{W}$

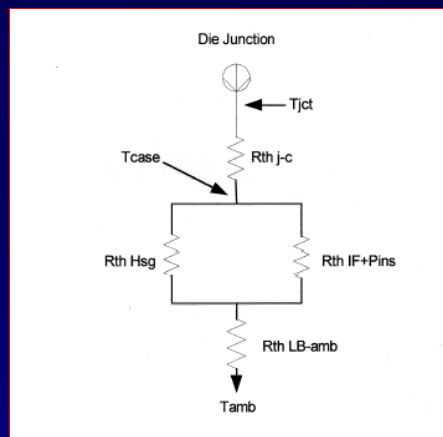
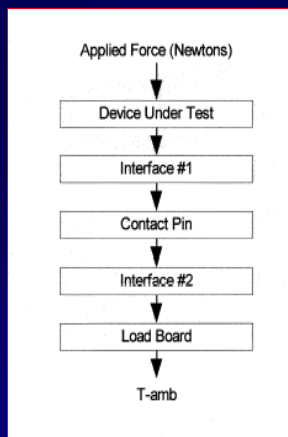
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## DUT $R_{th,x}$ Geometry for DUT-TS-LB

### Block and schematic diagrams of DUT $R_{th,x}$ geometry



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## Interface Evaluation & Thermal Rise

- Evaluation of IFs @  $V_{IN} = 20V$  and 40A
  - $V_{IF, Sn-BeCu} = 40A * 7.6 \times 10^{-4} \Omega / 3 \text{ pins} = 10mV/pin$
  - $V_{IF, Au-BeCu} = 40A * 1.3 \times 10^{-3} \Omega / 3 \text{ pins} = 13.4mV/pin$
  - Softening voltage is 70mV for tin and 80mV for gold
- Calculate S-S temp rise across contact pins
  - $\Delta T_{SS} = I^2 R / (m * c_p) = 40^2 * (1.1 \times 10^{-3} / 3) / (3 * 2.6 \times 10^{-6} * 418.7) = 171^\circ C$
  - $R_{th} = 150 / 3 = 50.0^\circ C/W$
  - $C_{th} = m * c_p = 3 * 262 \times 10^{-6} * 418.7 = 3.3 \times 10^{-3} \text{ W-sec}/^\circ C$
  - $\tau = R_{th} * C_{th} = 50.0 * 3.3 \times 10^{-3} = 165 \text{ milliseconds}$
  - $\Delta T_{pin} = 171 * (1 - \exp(-0.100 / 165)) = 0.1^\circ C$

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## Heat Generation in DUT & Mounting Base

- Apply a single-shot pulse of 800W peak for 100 microseconds
  - Duty cycle ( $\delta$ ) ~ 0
  - Apply graph from slide 16 – go to curve of ( $\delta$ ) ~ 0
  - $Z_{th, j-mb} = 0.1^\circ C/W$
  - $\Delta T_{j-mb} = P_{PEAK} * Z_{th, j-mb} = 800 * 0.1 = 80^\circ C$
- Determine temp of mounting base from thermal equation
  - Mass of metal =  $2.0 \times 10^{-5} \text{ Kg}$
  - $R_E = 8.6 \times 10^{-4} \Omega$
  - $\tau = 165 \times 10^{-3} \text{ secs}$
  - $T_{mb} = +25 + 171 * (1 - \exp(-1 \times 10^{-6} / 165 \times 10^{-3})) = 25^\circ C$
- Calculate the temp of the die junction
  - $T_{j,die} = T_{mb} + \Delta T_{j-mb} = +25 + 80 = 105^\circ C < 175^\circ C$

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## Conclusions

- Generally, reducing the duty cycle of a current pulse applied to a conductor reduces its internal temperature rise
- Transient analysis can be done in several ways...
  - By using the equations presented herein
  - By using a thermal Z vs. pulsed DC graph
- Application of a high peak power pulse of short duration to a power MOSFET is possible w/o damage to the device, providing:
  - Applied pulse is single-shot and of short duration (Duty cycle  $\sim 0$ )
  - Repetition time of pulse is very long (several seconds)
  - Breakdown voltage of the device is not violated
- Examples and most data in this presentation are calculated

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## Glossary Of Terms

### Terms and Units used in Heat Transfer

– Heat flux	J/m <sup>2</sup> -s
– Heat transfer rate	dQ = qA(W/m <sup>2</sup> )
– Mass density, $\rho$	Kg/m <sup>3</sup>
– Specific heat, $c_p$	J/Kg-K
– Thermal conductivity, k	W/m-K
– Thermal energy	Q(Joules)
– Thermal resistance, $R_{TH}$	°C/W
– Thermal capacitance, $C_{TH}$	W-sec/°C
– Thermal time constant, $\gamma$ or $\tau$	seconds

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### Appendix A: Thermal Characteristics of Materials

Material	Conductivity	Specific Heat
Silver	429.0 W/m-K	325 J/Kg-K
Copper	401.0	384
Gold	319.0	129
Aluminum	237.0	903
Tungsten	173.0	125
Nickel	90.4	444
Beryllium-Copper	90.0	420
Iron	80.4	450
Platinum	71.6	133
Tin	66.8	227
Lead	35.3	128

Source: Ruben, S., *Handbook Of The Elements* (Open Court: La Salle, IL 1996)

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### Appendix B: Softening/Melting Voltages

Material	Softening Volts (V)	Melting Volts (V)
Aluminum	0.10	0.30
Iron	0.19	0.19
Nickel	0.16	0.16
Copper	0.12	0.43
Zinc	0.10	0.17
Silver	0.09	0.37
Cadmium	0.15	---
Tin	0.07	0.13
Gold	0.08	0.43
Palladium	0.57	0.57
Lead	0.12	0.19
60Cu,40Zn	0.20	---

Source: Timron Scientific Inc., *Electrical Contacts And Electroplates In Separable Connectors*

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## **Appendix C: Critical Factors of Thermal Paths**

- Pressure at the interface
- Hardness of the contact surfaces
- Size of the contact surface asperities
- Geometry of contacting surfaces
- Average gap thickness of void spaces
- Thermal conductivity of fluid in void spaces
- Thermal conductivity of contact materials